Maths Progression Documents

Planning shows a clear sequential progression from concrete to pictorial to abstract so that our pupils gain a secure and deep learning of all concepts in maths. Progression in the teaching of calculation is displayed within our Calculation Policy, which has been carefully planned to ensure sequential learning is embedded across year groups so that children always build on prior knowledge when learning a new concept. Calculation methods are taught across the school by linking manipulatives with formal and informal methods, e.g., use of ten grids leading to pictorial methods then to formal addition and subtraction: number lines leading to mental methods.

The progression documents show key knowledge and skills from EYFS – Year 6.

			EYFS Mathematics		
	Number	Number facts	Numerical Patterns	Measure, Shape and Space	Vital Vocabulary
•	Have a deep understanding of number to 10, including the composition of each number; Subitise (recognise quantities without counting) up to 5	Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10, including double facts.	 Verbally count beyond 20, recognising the pattern of the counting system; Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity; Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally. 	Safely use and explore a variety of materials, tools and techniques, experimenting with colour, design, texture, form and function; including measuring. Recognise a range of shapes and link items that have the same shape.	Use enriching and widening children's vocabulary that will support later reading comprehension
	CountRead and writeIdentifyRepresent	RecallCountAddSubtract	CountCompareExploreRepresent	UseExploreRecognise	Use Explore

		Progression	on of knowledge and skills	 Number and place value 		
Strand	1	2	3	4	5	6
Number and place value	 count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number count, read and write numbers to 100 in numerals; count in multiples of 2s, 5s and 10s given a number, identify 1 more and 1 less identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least read and write numbers from 1 to 20 in numerals and words 	 count in steps of 2, 3, and 5 from 0, and in 10s from any number, forward and backward recognise the place value of each digit in a two-digit number (10s, 1s) identify, represent and estimate numbers using different representations, including the number line compare and order numbers from 0 up to 100; use <, > and = signs read and write numbers to at least 100 in numerals and in words use place value and number facts to solve problems 	 count from 0 in multiples of 4, 8, 50 and 100; find 10 or 100 more or less than a given number. recognise the place value of each digit in a 3-digit number (100s, 10s, 1s) compare and order numbers up to 1,000 identify, represent and estimate numbers using different representations read and write numbers up to 1,000 in numerals and in words solve number problems and practical problems involving these ideas 	 count in multiples of 6, 7, 9, 25 and 1,000 identify 1,000 more or less than a given number count backwards through 0 to include negative numbers recognise the place value of each digit in a four-digit number (1,000s, 100s, 10s, and 1s) order and compare numbers beyond 1,000 identify, represent and estimate numbers using different representations round any number to the nearest 10, 100 or 1,000 solve number and practical problems that involve all of the above and with increasingly large positive numbers read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of 0 and place value 	 read, write, order and compare numbers to at least 1,000,000 and determine the value of each digit count forwards or backwards in steps of powers of 10 for any given number up to 1,000,000 interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through 0 round any number up to 1,000,000 to the nearest 10, 100, 1,000, 10,000 and 100,000 solve number problems and practical problems that involve all of the above read Roman numerals to 1,000 (M) and recognise years written in Roman numerals 	 read, write, order and compare numbers up to 10,000,000 and determine the value of each digit round any whole number to a required degree of accuracy use negative numbers in context, and calculate intervals across 0 solve number and practical problems that involve all of the above
Skills	 Count Read and write Identify Represent Use Solve 	 Count Read and write Identify Recognise Represent Use Compare and order Solve 	 Count Read and write Identify Recognise Represent Use Compare and order Estimate Solve 	 Count Read and write Identify Recognise Represent Compare and order Estimate Solve Round 	 Count Read and write Identify Recognise Represent Compare and order Estimate Solve Round Determine Interpret 	 Read and write Identify Recognise Calculate Compare and order Estimate Solve Round Determine Use

		Progressio	n of knowledge and skills -	- Addition and Subtraction		
Strand	1	2	3	4	5	6
Addition and Sutraction	 read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs represent and use number bonds and related subtraction facts within 20 add and subtract one-digit and two-digit numbers to 20, including 0 solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = ? - 9 	solve problems with addition and subtraction: using concrete objects and pictorial representations, including those involving numbers, quantities and measures applying their increasing knowledge of mental and written methods recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 add and subtract numbers using concrete objects, pictorial representations, and mentally, including: a two-digit number and 10s 2 two-digit numbers adding 3 one-digit numbers adding 3 one-digit numbers show that addition of 2 numbers can be done in any order (commutative) and subtraction of 1 number from another cannot recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems	 add and subtract numbers mentally, including: a three-digit number and 1s a three-digit number and 10s a three-digit number and 100s add and subtract numbers with up to 3 digits, using formal written methods of columnar addition and subtraction estimate the answer to a calculation and use inverse operations to check answers solve problems, including missing number facts, place value, and more complex addition and subtraction 	add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate estimate and use inverse operations to check answers to a calculation solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why	add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) add and subtract numbers mentally with increasingly large numbers use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why	 perform mental calculations, including with mixed operations and large numbers use their knowledge of the order of operations to carry out calculations involving the 4 operations solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why solve problems involving addition and subtraction use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy
Skills	 Read and write Interpret Represent Use Add Subtract Solve 	o Recall o Check o Represent o Use o Add o Subtract o Solve o Apply o Mental methods o Prove (show) o Inverse	o Add o Subtract o Use o Solve o Apply o Mental methods o Formal methods o Prove (show) o Inverse o Estimate o Calculate	o Add o Subtract o Use o Solve o Apply o Mental methods o Formal methods o Prove/explain (why) o Inverse o Estimate O Calculate O Determine/decide	o Add o Subtract o Use o Solve o Apply o Mental methods o Formal methods o Prove/explain (why) o Inverse o Estimate O Calculate O Determine/decide	o Add o Subtract o Use o Solve o Apply o Mental methods o Formal methods o Prove/explain (why) o Inverse o Estimate O Calculate O Determine/decide

	Progr	ession of knowledge and ski	lls – Multiplication and Divis	sion	
Strand 1	2	3	4	5	6
solve one-step problems involving multiplication and division, by calculating the answ using concrete objects, pictorial representations and arrays with the support of the teach Multiplicati on and Division	calculate mathematical statements for multiplication and division within the	 recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects 	 recall multiplication and division facts for multiplication tables up to 12 × 12 use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together 3 numbers recognise and use factor pairs and commutativity in mental calculations multiply two-digit and three-digit numbers by a one-digit number using formal written layout solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by 1 digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects 	 identify multiples and factors, including finding all factor pairs of a number, and common factors of 2 numbers know and use the vocabulary of prime numbers, prime factors and composite (nonprime) numbers establish whether a number up to 100 is prime and recall prime numbers up to 19 multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers multiply and divide numbers mentally, drawing upon known facts divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context multiply and divide whole numbers and those involving decimals by 10, 100 and 1,000 recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3) solve problems involving the four operations, including using their knowledge of factors and multiples, squares and cubes; including scaling by simple fractions and problems involving simple rates 	 multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context perform mental calculations, including with mixed operations and large numbers identify common factors, common multiples and prime numbers use their knowledge of the order of operations to carry out calculations involving the 4 operations solve problems involving multiplication and division use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy

Skills	0	Solve	0	Recall	0	Recall	0	Recall	0	Identify	0	Identify
JKIIIS	0	Represent	0	Use	0	Multiplication	0	Multiplication	0	Multiplication	0	Multiplication
	0	Multiplication	0	Multiplication	0	Division	0	Division	0	Division	0	Division
	0	Division	0	Division	0	Recognise	0	Recognise	0	Recognise	0	Recognise
	0	Calculate	0	Recognise	0	Write	0	Write	0	Know and use	0	Know and use
			0	Write	0	Formal/mental methods						
			0	Show	0	Scaling	0	Scaling	0	Scaling	0	Scaling
			0	Solve	0	Solve	0	Solve	0	Solve	0	Solve
					0	Calculate	0	Calculate	0	Calculate	0	Estimate/calculate/check

Progression of Knowledge and Skills – Fractions, Decimals and Percentages											
Strand	1	2	3	4	5	6					
FDP	recognise, find and name a half as 1 of 2 equal parts of an object, shape or quantity recognise, find and name a quarter as 1 of 4 equal parts of an object, shape or quantity	 recognise, find, name and write fractions third, quarter, two-quarters and three-quarters of a length, shape, set of objects or quantity write simple fractions 	count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators recognise and show, using diagrams, equivalent fractions with small denominators add and subtract fractions with the same denominator within one whole compare and order unit fractions, and fractions with the same denominators solve problems that involve all of the above	recognise and show, using diagrams, families of common equivalent fractions count up and down in hundredths; recognise that hundredths arise when dividing an object by 100 and dividing tenths by 10 solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including nonunit fractions where the answer is a whole number add and subtract fractions with the same denominator recognise and write decimal equivalents of any number of tenths or hundreds recognise and write decimal equivalents to quarter, half and three-quarters find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths round decimals with 1 decimal place to the nearest whole number compare numbers with the same number of decimal places up to 2 decimal places solve simple measure and money problems involving fractions and decimals to 2 decimal places	 compare and order fractions whose denominators are all multiples of the same number identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number add and subtract fractions with the same denominator, and denominators that are multiples of the same number multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams read and write decimal numbers as fractions recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents round decimals with 2 decimal places to the nearest whole number and to 1 decimal place read, write, order and compare numbers with up to 3 decimal places solve problems involving number up to 3 decimal places recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per 100', and write percentages as a fraction with denominator 100, and as a decimal fraction solve problems which require knowing percentage and decimal equivalents of half, quarter, fifth, two-fifths, four-fifths and those fractions with denominators of multiples of 10 or 25. 	 use common factors to simplify fractions; use common multiples to express fractions in the same denomination compare and order fractions, including fractions >1 add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions multiply simple pairs of proper fractions, writing the answer in its simplest form divide proper fractions by whole numbers associate a fraction with division and calculate decimal fraction equivalents (for example, 0.375) for a simple fraction identify the value of each digit in numbers given to 3 decimal places and multiply and divide numbers by 10, 100 and 1,000 giving answers up to 3 decimal places multiply one-digit numbers with up to 2 decimal places multiply one-digit numbers with up to 2 decimal places by whole numbers use written division methods in cases where the answer has up to 2 decimal places solve problems which require answers to be rounded to specified degrees of accuracy recall and use equivalences between simple fractions, decimals and percentages, including in different contexts 					
Skills	RecogniseFindName	RecogniseFindName	CountFind/Recognise	Count Recognise/identify	CountRecognise/identify	Count Recognise/identify/recall					

○ Write	 Find Write Use/solve Show Add/subtract fractions Compare and order 	 Find Write Use (including diagrams) Show Add/subtract fractions Solve/calculate Compare 	 Find Write Use (including diagrams) Show Add/subtract fractions Solve/calculate Compare/order 	 Find Write Use (including diagrams) Show Add/subtract fractions Solve/calculate Compare/order

		Progre	ssion of Knowledge and Sk	ills – Measurement		
Strand	1	2	3	4	5	6
Measureme nt	 compare, describe and solve practical problems for: length and heights, mass/weight, capacity and volume, time. measure and begin to record the following: length and heights, mass/weight, capacity and volume, time. recognise and know the value of different denominations of coins and notes sequence events in chronological order using language [for example, before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] recognise and use language relating to dates, including days of the week, weeks, months and years tell the time to the hour and half past the hour and draw the hands on a clock face to show these times 	 choose and use appropriate standard units to estimate and measure length/height in any direction (m/cm); mass (kg/g); temperature (°C); capacity (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels compare and order lengths, mass, volume/capacity and record the results using >, < and = recognise and use symbols for pounds (£) and pence (p); combine amounts to make a particular value find different combinations of coins that equal the same amounts of money solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change compare and sequence intervals of time tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times know the number of minutes in an hour and the number of hours in a day 	 measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml) measure the perimeter of simple 2-D shapes add and subtract amounts of money to give change, using both £ and p in practical contexts tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes and hours; use vocabulary such as o'clock, am/pm, morning, afternoon, noon and midnight know the number of seconds in a minute and the number of days in each month, year and leap year compare durations of events 	 convert between different units of measure measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres find the area of rectilinear shapes by counting squares estimate, compare and calculate different measures, including money in pounds and pence read, write and convert time between analogue and digital 12- and 24-hour clocks solve problems involving converting from hours to minutes, minutes to seconds, years to months, weeks to days 	 convert between different units of metric measure understand and use approximate equivalences between metric units and common imperial units measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres calculate and compare the area of rectangles (including squares), including using standard units, square centimetres (cm²) and square metres (m²), and estimate the area of irregular shapes estimate volume and capacity solve problems involving converting between units of time use all four operations to solve problems involving measure [for example, length, mass, volume, money] using decimal notation, including scaling 	 solve problems involving the calculation and conversion of units of measure, using decimal notation up to 3 decimal places where appropriate use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to 3 decimal places convert between miles and kilometres recognise that shapes with the same areas can have different perimeters and vice versa recognise when it is possible to use formulae for area and volume of shapes calculate the area of parallelograms and triangles calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm³) and cubic metres (m³), and extending to other units
Skills	 Compare and describe Solve Measure Recognise Know Use 	Choose and use Estimate and measure Compare and order Recognise Find and know Solve	Measure Compare Tell and write the time Estimate Know	Measure Compare Read, tell and write the time Estimate Convert Solve	Measure Compare Read, tell and write the time Estimate Convert Solve	 Use, read and write Compare Convert Estimate Convert Solve

		Pro	gression of Knowledge an	d Skills – Geometry		
Strand	1	2	3	4	5	6
Geometry – Properties of shapes	recognise and name common 2-D and 3-D shapes, including: 2-D shapes [for example, rectangles (including squares), circles and triangles] 3-D shapes [for example, cuboids (including cubes), pyramids and spheres]	 identify and describe the properties of 2-D shapes, including the number of sides, and line symmetry in a vertical line identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid] compare and sort common 2-D and 3-D shapes and everyday objects 	 draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them recognise angles as a property of shape or a description of a turn identify right angles, recognise that 2 right angles make a half-turn, 3 make three-quarters of a turn and 4 a complete turn; identify whether angles are greater than or less than a right angle identify horizontal and vertical lines and pairs of perpendicular and parallel lines 	compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes identify acute and obtuse angles and compare and order angles up to 2 right angles by size identify lines of symmetry in 2-D shapes presented in different orientations complete a simple symmetric figure with respect to a specific line of symmetry	 identify 3-D shapes, including cubes and other cuboids, from 2-D representations know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles draw given angles, and measure them in degrees (°) identify: angles at a point and 1 whole turn (total 360°) angles at a point on a straight line and half a turn (total 180°) other multiples of 90° use the properties of rectangles to deduce related facts and find missing lengths and angles distinguish between regular and irregular polygons based on reasoning about equal sides and angles 	 draw 2-D shapes using given dimensions and angles recognise, describe and build simple 3-D shapes, including making nets compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles
Geometry – Position and direction	describe position, direction and movement, including whole, half, quarter and three-quarter turns	order and arrange combinations of mathematical objects in patterns and sequences use mathematical vocabulary to describe position, direction and movement, including movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anti-clockwise)	Pupils connect decimals and rounding to drawing and measuring straight lines in centimetres, in a variety of contexts. (Non-statutory)	describe positions on a 2-D grid as coordinates in the first quadrant describe movements between positions as translations of a given unit to the left/right and up/down plot specified points and draw sides to complete a given polygon	identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed	describe positions on the further coordinate grid (all 4 quadrants) draw and translate simple shapes on the coordinate plane, and reflect them in the axes
Skills	RecogniseNameDescribe	 Identify Describe Compare Sort Order and arrange Use Distinguish 	 Draw Recognise Identify Connect 	 Classify Compare Identify Complete symmetry Describe Plot 	 Draw and know Recognise and describe Build Compare and classify Illustrate and name Distinguish Represent 	 Draw Recognise and describe Build Compare and classify Illustrate and name Translate

as and anawers imple questions by counting the number of objects in each category and so ground in each category and so ground in the categories by quantity as and anawer questions about totalling and companing categorical data Statistics (Y2, 3, 4, 5 and 6) Ratio and proportion – Y6 ONLY Algebra – Year 6 ONLY Alge			Progression of	Knowledge and Skills – Statistic	cs (Y2-6) Ratio and Proportion (Y6) Algebra (Y6)	
pictograms, and tables diagrams and tables solve one-step and two-step solve one-step and two-step solve one-step and two-step in each category and sorting the categories in each category and sorting the categories of yournity counting the number of objects in each category and sorting the categories of yournity counting the number of objects in each category and sorting the categories in each category and sorting the categories in each category and sorting the categories of yournity counting the number of objects in each category and sorting the categories of yournity counting the number of objects in each category and sorting the categories of yournity counting the number of objects in each category and sorting the categories and each proportion— Ye ONLY Algebra - Year 6 ONLY ONLY Algebra - Year 6 ONLY Alg	Strand	_			_ · _ · _ ·		6
can be found by using integer multiplication and division facts solve problems involving the calculation of percentages [for example, as fast of 360] and the use of percentages for comparison solve problems solve problems	Statistics (Y2, 3, 4, 5 and 6) Ratio and proportion – Y6 ONLY Algebra – Year	_	interpret and construct simple pictograms, tally charts, block diagrams and tables ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity ask-and-answer questions about totalling and comparing categorical	interpret and present data using bar charts, pictograms and tables solve one-step and two-step questions [for example 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms	interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and	solve comparison, sum and difference problems using information presented in a line graph complete, read and interpret information in tables, including	• interpret and construct pie charts and line graphs and use these to solve problems • calculate and interpret the mean as an average Algebra • use simple formulae • generate and describe linear number sequences • express missing number problems algebraically • find pairs of numbers that satisfy an equation with 2 unknowns • enumerate possibilities of combinations of 2 variables Ratio and Proportion • solve problems involving the relative sizes of 2 quantities
where the scale factor is							can be found by using integer multiplication and division facts • solve problems involving the calculation of percentages [for example, of measures and such as 15% of 360] and the use of percentages for comparison • solve problems involving similar shapes

							using knowledge of fractions and multiples
Skills	InterpretConstruct	InterpretPresent	InterpretPresent	0 0	Complete Read	0 0	Interpret Construct
	 Ask and answer 	o Solve	o Solve	0	Interpret	0	Use
				0	Solve	0	Generate and describe
						0	Express
						0	Find
						0	Enumerate
						0	Solve